Coding Categorical Predictors for LSA 2013, LI539 Mixed Effect Models

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Introduction

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Coding Schemes

Treatment Coding Effects Coding Helmert Coding Polynomial Coding

Adding Interactions

Interactions of Categorical Variables Interactions of Continuous and Categorical Variables More About In-

Auxiliary lecture 1: Coding of categorical predictors

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References

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Interactions of Categorical Variables Interactions of Continuous and Categorical Variables More About Interactions Cohen, & Cohen, (1983). Applied multiple regression/correlation analysis for the behavioral sciences.

• Especially chapters 8 & 9

Kaufman, D. & Sweet, R. (1974). Contrast coding in least squares regression analysis. *American Educational Research Journal*, *11*, 359–377.

Serlin, R. C., & Levin, J. R. (1985). Teaching how to derive directly interpretable coding schemes for multiple regression analysis. *Journal of Educational Statistics*, *10*, 223–238.

Wendorf, C. A. (2004). Primer on multiple regression coding: Common forms and the additional case of repeated contrasts. *Understanding Statistics*, *3*, 47–57

4 **D b** 4 **d b** 4 **d b** 4

How do we treat categorical variables in regression?

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Adding Interactions

Interactions of Categorical Variables Interactions of Continuous and Categorical Variables More About In• As sets of IVs (code variables)

• Together they represent the full information from original categories.

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Multiple ways to set up code variables

- Different ways test different predictions
- These are essentially planned comparisons

How do we treat categorical variables in regression?

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• Together they represent the full information from original categories.

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- Multiple ways to set up code variables
 - Different ways test different predictions
 - These are essentially planned comparisons

How many coding variables are necessary?

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Interactions of Categorical Variables Interactions of Continuous and Categorical Variables More About InFor any grouped/non-continuous IV (**G**) with some number of levels (g), g - 1 coding variables are needed to represent **G**.

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• 4 levels \rightarrow 3 coding variables (C_1 , C_2 , C_3)

- 3 levels \rightarrow 2 coding variables (C_1 , C_2)
- 2 levels \rightarrow 1 coding variables (C₁)

NB:

g - 1 = # of degrees of freedom (df) of **G**

How do we represent the coding variables?

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Basic

Concepts

Coding

Coding

of Categorical

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About In-

Common coding systems

- Treatment/Dummy Coding
- Effects/Sum Coding
- Helmert Coding
- Polynomial Coding

NB:

The choice of your coding scheme affects the interpretation of the results for each **individual coding variable**; however, it does not change the **overall effect** of the set of coding variables (i.e., model fit and related statistics will not be affected).

Example Data Set

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- Word status
 - /smok/ = word
 - /plok/ = phonologically legal nonword
 - /lbok/ = phonologically illegal nonword
- Task: Press button if the item is or sounds like an English word.

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• DV: RT of response.

Read in Data

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```
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Effects
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Helmert
Coding
Polynomial
Coding
```

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```
library(languageR)
library(lme4)
d<-read.table("data/fakedata.txt", header=TRUE)
#renames factors
d$IV1<-ifelse(d$IV1==1, "silent", "noise")
d$IV2<-ifelse(d$IV2==2, "word", ifelse(d$IV2==3, "legal", "illegal"))
d$NoiseCond<-as.factor(d$IV1)
d$WordCond<-as.factor(d$IV2)
d$WordCond<-as.factor(d$VrdCond)
d$NoiseCond<-as.factor(d$Freq)
head(d)</pre>
```

##		Subject	Item	IV1	IV2	Response	RT	Freq	NoiseCond	WordCond
##	1	1	1	${\tt silent}$	word	1	762	0.24	silent	word
##	2	1	2	${\tt silent}$	word	1	608	5.22	silent	word
##	3	1	3	silent	word	1	744	5.10	silent	word
##	4	1	4	${\tt silent}$	word	1	609	5.77	silent	word
##	5	1	9	${\tt silent}$	word	1	965	2.37	silent	word
##	6	1	10	${\tt silent}$	word	1	817	5.80	silent	word

Condition Means

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attach(d) #RT means for single WordCond variable

x

RTmeans<-aggregate(RT, list(WordCond), FUN=mean)

#RT means for two variables (WordCond and NoiseCond - used in interactions.)

RTmeansWN<-aggregate(RT, list(WordCond, NoiseCond), FUN = mean)

```
Introductio
```

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RTmeans

Group.1

1 illegal 1315.5

##

Coding Schemes Treatment Coding Effects Coding Helmert Coding

Polynomial Coding

Adding Interactior

Interactions of Categorical Variables Interactions of Continuous and Categorical Variables More About Intoractions ## 2 legal 969.7 ## 3 word 731.7 RTmeansWN Group.1 Group.2 ## X ## 1 illegal noise 1462.3 ## 2 legal noise 1035.5 ## 3 word noise 738.3 ## 4 illegal silent 1168.7 ## 5 legal silent 903.9 ## 6 word silent 725.1

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Example Data Set

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Lexical Decision Task

• Does word status affect the time to make responses?

We'll run linear mixed-effect models testing this general question with different coding schemes.

• One fixed effect (WordCond) and two random effects (Subject and Item intercepts)

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Interactions of Categorical Variables Interactions of Continuous and Categorical Variables More About InCompares other groups to a reference group.

- Considerations for choosing a reference group
 - Useful comparison (e.g., control, predicted highest or lowest)

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- Well-defined group (e.g., not a catch-all category)
- Should not have small n compared to other groups
- Intercept represents the reference group mean.

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Interactions of Categorical Variables Interactions of Continuous and Categorical Variables More About InImagine the question we're interested in is whether responses to each of the nonword conditions differ from the *word* condition.

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Question

What level should we choose as a reference group?

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Adding Interactions

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We should choose *word* as our reference group.

- Reference group receives a value of 0 for all coding variables (C_i)
- Each other level receives 1 in one of the coding variables

Levels	\mathbf{C}_1	\mathbf{C}_2
word	0	0
legal	1	0
illegal	0	1

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C₁ tests legal against word **C**₂ tests illegal against word

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Interactions of Categorical Variables Interactions of Continuous and Categorical Variables More About In#Create column for treatment coded WordCond
d\$WordCond.Treatment<-d\$WordCond</pre>

R automatically assigns levels alphabetically, this isn't always #what you'll want, so you can reassign the order of the levels as #shown below...

d\$WordCond.Treatment<-factor(d\$WordCond.Treatment, levels=c("word","legal","illegal"))

#This line reorders levels to put "word" in baseline position (1st in list)

R's default is to set coding scheme to Treatment, so here you #don't need to do anything else now that the levels are ordered #appropriately.

#More generally, if you just want to specify which level is the #baseline you can do the following:

#contrasts(d\$WordCond.Treatment)<-contr.treatment(3, base=3)</pre>

#This says set the contrasts to treatment coding with 3 levels, #with the 3rd level being the base condition

lin.Treatment<-lmer(RT ~ WordCond.Treatment + (1|Subject) + (1|Item), data=d) #linear model

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Problem 1

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Task

- Choose a base group that tests this question.
- Set up this coding scheme in R.
- Run the model and interpret the coefficients.

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Adding Interactions

Interactions of Categorical Variables Interactions of Continuous and Categorical Variables More About In#Create column for treatment coded WordCond d\$WordCond.Treatment<-d\$WordCond</pre>

d\$WordCond.Treatment<-factor(d\$WordCond.Treatment, levels=c("word","legal","illegal"))

```
contrasts(d$WordCond.Treatment)<-contr.treatment(3, base=3)</pre>
```

Problem1<-lmer(RT ~ WordCond.Treatment + (1|Subject) + (1|Item), data=d) #linear model

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```
Problem1
```

```
## Linear mixed model fit by REML
## Formula: RT ~ WordCond.Treatment + (1 | Subject) + (1 | Item)
##
      Data: d
##
      AIC
            BIC logLik deviance REMLdev
    15582 15612 -7785
                          15590
                                  15570
##
   Random effects:
##
    Groups
##
             Name
                         Variance Std.Dev.
##
    Subject
            (Intercept) 1.39e-06 1.18e-03
##
    Item
             (Intercept) 3.03e+01 5.50e+00
##
    Residual
                         4 42e+04 2 10e+02
## Number of obs: 1152, groups: Subject, 24; Item, 8
##
## Fixed effects:
##
                       Estimate Std. Error t value
## (Intercept)
                         1315.5
                                       10.9
                                            120.7
## WordCond.Treatment1 -583.8
                                      15.2
                                              -38.5
## WordCond Treatment2
                         -345.8
                                       15.2
                                              -22.8
##
## Correlation of Fixed Effects:
##
               (Intr) WrC.T1
## WrdCnd.Trt1 -0.696
## WrdCnd.Trt2 -0.696 0.500
```

- Intercept: Illegal nonword mean RT is 1316ms.
- $\bullet~\textbf{C}_1:$ Legal nonwords are responded to 346ms faster than illegal nonwords.

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• C₂: Words are responded to 584ms faster than illegal nonwords.

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Adding Interactions

Interactions of Categorical Variables Interactions of Continuous and Categorical Variables More About InCompares mean of a single group to the grand mean.

- Usually useful for unordered experimental groups
- Base group is chosen
 - Choose "least" interesting group
- Sum of the contrast weights of the coding variables always equals 0.

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• Intercept represents the grand mean.

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Interactions of Categorical Variables Interactions of Continuous and Categorical Variables More About InImagine that we choose word as our base group.

- Base group receives a value of -1 for all coding variables (C_i)
- Each other level receives 1 in one of the coding variables

Levels	\mathbf{C}_1	C_2
word	-1	-1
legal	0	1
illegal	1	0

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 C_1 is the difference between illegal and grand mean. C_2 is the difference between the legal and grand mean.

teractions

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troduction Basic Concepts	
Example Data Set	d\$WordCond.Effects<-d\$WordCond
oding chemes	<pre>contrasts(d\$WordCond.Effects)<-cbind("illegal.v.GM"= c(1, 0, -1), "legal.v.GM"= c(0, 1, -1))</pre>
Freatment Coding Effects	<pre>#renames Cis to give indication of what is being tested #C1 = illegal vs. grandmean, C2= legal vs.grandmean</pre>
Coding Helmert Coding	<pre>lin.Effects<-lmer(RT ~ WordCond.Effects + (1 Subject) + (1 Item), data=d)</pre>
Polynomial Coding	
dding iteractions	
nteractions of Cate- gorical /ariables	
nteractions of Contin- ious and Categori- cal	
Variables More	

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```

Adding Interaction

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```
## Linear mixed model fit by REML
## Formula: RT ~ WordCond.Effects + (1 | Subject) + (1 | Item)
##
      Data: d
      AIC
            BIC logLik deviance REMLdev
##
##
    15584 15614 -7786
                          15590
                                  15572
## Random effects:
##
    Groups
             Name
                         Variance Std.Dev.
    Subject (Intercept) 1.39e-06 1.18e-03
##
##
    Ttem
             (Intercept) 3.03e+01 5.50e+00
                         4.42e+04 2.10e+02
##
    Residual
## Number of obs: 1152, groups: Subject, 24; Item, 8
##
## Fixed effects:
##
                                Estimate Std. Error t value
## (Intercept)
                                 1005.65
                                                6.49
                                                       154.9
## WordCond.Effectsillegal.v.GM 309.87
                                                       35.4
                                                8.76
## WordCond.Effectslegal.v.GM
                                  -35.95
                                               8.76
                                                      -4.1
##
## Correlation of Fixed Effects:
##
                       (Intr) WrdCnd.Effctsll..GM
## WrdCnd.Effctsll..GM 0.000
## WrdCnd.Effctslg..GM 0.000 -0.500
```

- Intercept: Grand mean RT is 1006ms.
- $\bullet~C_1:$ Illegal nonwords are responded to \sim 310ms slower than the grand mean.
- C₂: Legal nonwords are responded to ~ 37ms faster than the grand mean.

Orthogonal Contrast Coding

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Interactions of Categorical Variables Interactions of Continuous and Categorical Variables More About InGoal of these coding systems is to allow each coding variable (C_i) to

- capture unique portions of the variance (i.e., orthogonal).
- test specific, theory-guided hypotheses (i.e., planned comparisons).

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Constructing Orthogonal Contrast Codes (Cohen & Cohen, 1984)

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- **Rule 1.** The sum of the weights across each code variable (*C_i*) must equal 0.
- **Rule 2.** The sum of the products of each pair of code variable (*C*₁, *C*₂) must equal 0.
 - When group sizes are equal, this ensures that contrast codes are orthogonal (i.e., do not capture overlapping portions of the variance).
- **Rule/Suggestion 3.** The difference between the value of the set of positive weights and the value of the set of negatives weights should equal 1.
 - Allows each unstandardized β to correspond to the difference between the unweighted means of the groups involved in the contrast.

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Treatment Coding

Levels

Effects Coding

C

-1

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0

0

Co

-1

0

1

0

A D > A D > A D > A D >

 $\mathbf{C}_1\mathbf{C}_2$

= 1

= 0

= 0

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Levels

word

legal

illegal

sum

Basic
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Coding Coding Helmert

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 \mathbf{C}_2 $\mathbf{C}_1\mathbf{C}_2$ 0 word 0 = 0legal 1 0 = 0illegal 0 1 = 01 1 0 sum

C1

Violates Rule 1

Violates Rule 2

Whenever possible and predictions allow it, use orthogonal coding schemes.

Helmert Coding

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Adding Interactions

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- Useful for ordinal variables
- Example comparisons
 - Does Level 1 differ from Level 2?
 - Does Level 1 differ from the mean of Levels 2 & 3?

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• Intercept represents the grand mean.

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Adding Interaction

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More About Interactions Are real English words more quickly or more often perceived as words than nonwords?

Are listeners sensitive to phonotactics of nonwords such that they more quickly and more often perceive phonologically legal nonwords as words than phonologically illegal nonwords?

Levels	C_1	C_2
word	0	2/3
legal	1/2	-1/3
illegal	-1/2	-1/3

C₂ tests legal against illegal)

C₁ tests word against mean of legal and illegal (i.e., word vs. nonword)

NB:

R does not automatically assign weights that satisfy Rule/Suggestion 3.

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```
d$WordCond.Helm.Reg<-d$WordCond
```

```
contrasts(d$WordCond.Helm.Reg)<-
    cbind("leg.vs.ill"= c(-.5, .5, 0),
        "word.vs.nons"=c (-(1/3), -(1/3), (2/3))
}</pre>
```

#renames Cis to give indication of what is being tested... C1 = illegal vs. legal, #C2= word vs.nonwords(mean of other two levels)

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lin.Helm.Reg<-lmer(RT ~ WordCond.Helm.Reg + (1|Subject) + (1|Item), data=d)

Helmert Coding

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```
## Linear mixed model fit by REML
## Formula: RT ~ WordCond.Helm.Reg + (1 | Subject) + (1 | Item)
##
      Data: d
##
      AIC
            BIC logLik deviance REMLdev
    15582 15612 -7785
##
                          15590
                                  15570
  Random effects:
##
    Groups
                         Variance Std.Dev.
##
             Name
    Subject
            (Intercept) 1.39e-06 1.18e-03
##
##
    Ttem
             (Intercept) 3.03e+01 5.50e+00
##
    Residual
                         4.42e+04 2.10e+02
## Number of obs: 1152, groups: Subject, 24; Item, 8
##
## Fixed effects:
##
                                 Estimate Std. Error t value
## (Intercept)
                                  1005.65
                                                6.49
                                                      154.9
                                               15.17 -22.8
## WordCond.Helm.Regleg.vs.ill -345.83
## WordCond.Helm.Regword.vs.nons
                                  -410.87
                                               13.14
                                                     -31.3
##
## Correlation of Fixed Effects:
##
                    (Intr) WrdCnd.Hlm.Rgl..
## WrdCnd.Hlm.Rgl.. 0.000
## WrdCnd.Hlm.Rgw.. 0.000 0.000
```

 C_1 : Phonologically legal nonwords are responded to 346ms faster than phonologically illegal nonwords.

C₂: English words are responded to 411ms faster than nonwords.

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- Linear trend?
- Quadratic trend?
- Higher-level trends?

Can test for g - 1 higher-order trends.

- 2-level factor: Linear (X¹)
- 3-level factor: Linear, Quadratic (X^2)
- 4-level factor: Linear, Quadratic, Cubic (X^3)

NB:

Orthogonal polynomial contrasts can be automatically generated by R for any number of levels using the function contr.poly(n), where n = number of levels of your factor.

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How do we model trends in ordered, categorical variables?

d\$WordCond.Poly <- d\$WordCond

```
contrasts(d$WordCond.Poly)<- contr.poly(3)</pre>
```

lin.Poly<- lmer(RT~WordCond.Poly + (1|Subject) + (1|Item), data=d)

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 C_1 (.L) tests if there is a linear component. C_2 (.Q) tests if there is a quadratic trend.

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More About Interactions lin.Poly

```
## Linear mixed model fit by REML
## Formula: RT ~ WordCond.Poly + (1 | Subject) + (1 | Item)
##
      Data: d
      ATC
##
            BIC logLik deviance REMLdev
##
    15583 15613 -7785
                          15590
                                   15571
## Bandom effects:
##
    Groups
             Name
                         Variance Std.Dev.
             (Intercept) 1.39e-06 1.18e-03
    Subject
##
##
    Item
             (Intercept) 3.03e+01 5.50e+00
    Residual
                         4.42e+04 2.10e+02
##
## Number of obs: 1152, groups: Subject, 24; Item, 8
##
## Fixed effects:
                   Estimate Std. Error t value
##
##
  (Intercept)
                    1005.65
                                   6.49
                                          154.9
## WordCond.Polv.L -412.80
                                  10.73
                                          -38.5
## WordCond.Poly.Q
                    44.04
                                  10.73
                                            4.1
##
## Correlation of Fixed Effects:
##
               (Intr) WC.P.L
## WrdCnd.Pl.L 0.000
## WrdCnd.Pl.Q 0.000 0.000
```

C₁: Significant linear trend. **C**₂: Significant quadratic trend.

Coding Categorical Predictors for LSA 2013, LI539 Mixed Effect Models

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July 5, 2013

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Auxiliary lecture 2: Interactions

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Interactions with Categorical Variables

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- "Difference of differences" when looking at interactions with two (or more) categorical variables.
- Differences among slopes when looking at interactions with a categorical variable and a continuous variable.

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• Choice of coding scheme affects interpretation of β s and intercept

Example Data Set - Categorical × Categorical

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Lexical Decision Task

- WordCond: /smok/ > /plok/ > /lbok/
 - /smok/ = word
 - /plok/ = phonologically legal nonword
 - /lbok/ = phonologically illegal nonword
- NoiseCond: Noise vs. Silence
- Task: Press button if the item sounds like or is an English word.

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• DV: Response Time (RT)

Mean RT (ms) by Word Condition and Noise Condition



About In-

	Word	Legal	Illegal
Noise	738	1035	1462
Silence	725	904	1169

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Interactions of Categorical Variables

Interactions of Continuous and Categorical Variables More About Interactions Reference group receives a value of 0 for all coding variables (C_i)

• We'll choose *word* as our reference group for WordCond and *noise* as our reference group for NoiseCond

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Each other level receives 1 in one of the coding variables

Levels	WC_1	WC_2	Levels	NC_1
word	0	0	noise	0
legal	1	0	silent	1
illegal	0	1		

NB:

Intercept represents the mean of the noise-word condition

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Interactions of Continuous and Categorical Variables More About Ind\$NoiseCond.Treatment <- d\$NoiseCond

contrasts(d\$NoiseCond.Treatment)<-contr.treatment(2)
contrasts(d\$WordCond.Treatment)<-contr.treatment(3)</pre>

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R's default is to treatment code

l.Treatment.int<-lmer(RT ~
NoiseCond.Treatment*WordCond.Treatment +
(1|Subject) + (1|Item), data=d)</pre>

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of Continuous and Categorical Variables More About Interactions

## Linear mixed model fit by REML	
## Formula: RT ~ NoiseCond.Treatment * WordCond.Treatment + (1 Subject) + (1	Item)
## Data: d	
## AIC BIC logLik deviance REMLdev	
## 15314 15359 -7648 15338 15296	
## Random effects:	
## Groups Name Variance Std.Dev.	
## Subject (Intercept) 0.0 0.00	
## Item (Intercept) 90.2 9.49	
## Residual 35588.6 188.65	
## Number of obs: 1152, groups: Subject, 24; Item, 8	
##	
## Fixed effects:	
## Estimate Std. Error t value	
## (Intercept) 738.3 14.0 52.7	
## NoiseCond.Treatment2 -13.2 19.3 -0.7	
## WordCond.Treatment2 297.1 19.3 15.4	
## WordCond.Treatment3 724.0 19.3 37.6	
## NoiseCond.Treatment2:WordCond.Treatment2 -118.4 27.2 -4.3	
## NoiseCond.Treatment2:WordCond.Treatment3 -280.4 27.2 -10.3	
##	
## Correlation of Fixed Effects:	
## (Intr) NsC.T2 WrC.T3 NC.T2:WC.T2	
## NsCnd.Trtm2 -0.687	
## WrdCnd.Trt2 -0.687 0.500	
## WrdCnd.Trt3 -0.687 0.500 0.500	
## NC.T2:WC.T2 0.485 -0.707 -0.707 -0.354	
## NC.T2:WC.T3 0.485 -0.707 -0.354 -0.707 0.500	

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Interpretation of Treatment Coding Model

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	Word	Legal	Illegal
Noise	738	1035	1462
Silence	725	904	1169

- Intercept (738) = Noise-Word Condition
- NoiseCondsilent (-13) = Silence-Word Noise-Word
- WordCondlegal (297) = Noise-Legal Noise-Word
- WordCondlegal (724) = Noise-Illegal Noise-Word
- NCsil*WCleg (-118)= (Silence-Legal Noise-Legal) (Silence-Word Noise-Word)
- NCsil:WCill (-280) = (Silence-Illegal Noise-Illegal) (Silence-Word Noise-Word)

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Comparison of models with different coding schemes

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Each complete set of coding variables captures the same overall proportion of the variance in the DV, but the interpretation of each individual β is different under different coding schemes.

This means that significance of each individual coefficient can vary depending on the chosen coding scheme; however, overall significance of an effect (equivalent to main effects and interactions in an ANOVA) remains the same.

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Example Data Set - Continuous \times Categorical

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More About Interactions Lexical Decision Task

- c.Freq: Centered log Freq
- WordCond: Word vs. Legal Nonword vs. Illegal Nonword
- Task: Press button if the item sounds like an English word.

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• DV: Response Time (RT)

Example Data Set - Continuous × Categorical

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Illegal: -12.6ms/unitFreq Legal: -7.4ms/unitFreq Word: 1.6ms/unitFreq

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More About Interactions Imagine we want to know whether the effect of phoneme frequency differed between words and nonwords.

- Reference group receives a value of 0 for all coding variables (C_i)
 - We'll choose word as our reference group for WordCond
- Each other level receives 1 in one of the coding variables

Levels	WC_1	WC_2	Continuous Variable
word	0	0	Continuous Variable
legal	1	0	c. Fred (centered log frequency)
illegal	0	1	

NB:

Intercept represents the mean of the word condition at the mean frequency.

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ntroduction						
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Coding Schemes	d\$c.Freq<-d\$Freq-mean(d\$Freq)					
Treatment Coding	<pre>l.Treatment.cont.c<-lmer(RT ^</pre>	c.Freq*WordCond.Tre	atment + (1 Subje	ect) + (1 It	em), data=d)	
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Schemes Treatment Coding Effects Coding Helmert Coding Polynomial Coding Adding

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More About Interactions 1.Treatment.cont.c

Linear mixed model fit by REML ## Formula: RT ~ c.Freq * WordCond.Treatment + (1 | Subject) + (1 | Item) ## Data: d ATC ## BIC logLik deviance REMLdev 15559 15604 -7770 ## 15574 15541 ## Bandom effects: ## Groups Name Variance Std.Dev. Subject (Intercept) 5,13e-07 7,16e-04 ## ## Item (Intercept) 3.63e+01 6.02e+00 4.37e+04 2.09e+02 ## Residual ## Number of obs: 1152, groups: Subject, 24; Item, 8 ## ## Fixed effects: Estimate Std. Error t value ## 67.3 ## (Intercept) 731.73 10.88 0.5 ## c.Freq 1.71 3.69 ## WordCond.Treatment2 238.11 15.09 15.8 ## WordCond Treatment3 583.50 15.09 38.7 ## c.Freg:WordCond.Treatment2 -8.92 5.20 -1.7 ## c.Freq:WordCond.Treatment3 -14.285.23 -2.7## ## Correlation of Fixed Effects: ## (Intr) c.Freq WrC.T2 WrC.T3 c.F:WC.T2 ## c.Freq -0.001## WrdCnd Trt2 -0.694 0.001 ## WrdCnd.Trt3 -0.694 0.001 0.500 ## c.Frg:WC.T2 0.001 -0.709 -0.004 -0.001 ## c.Frg:WC.T3 0.001 -0.705 -0.001 0.003 0.500

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Interpretation of Treatment Coding Model

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More About Interactions c.Freq: In word condition, for every unit increase in log frequency, RT is 1.7ms slower.

WC2: Legal nonwords are responded to 238ms slower than words.

WC3: Illegal nonwords are responded to 584ms slower than words.

c.Freq*WC2: The frequency effect in the legal condition is non-significantly in the opposite direction of the frequency effect in word condition (legal freq effect: 1.71 + (-8.92) = -7.2ms/unit Freq).

c.Freq*WC3: The frequency effect in the illegal condition is significantly in the opposite direction of the frequency effect in word condition (illegal freq effect: 1.71 + (-14.28) = -12.6ms/unit Freq).

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But do I have an omnibus interaction?

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More About Interactions Usually theoretical predictions do not concern the presence of an omnibus interaction involving multi-level categorical predictors.

- If you're using ANOVA, the presence of an omnibus interaction provides justification to test comparisons of theoretical interest.
- In regression, you can often code your variables in a way to test these specific hypotheses.

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If you want to determine whether the omnibus interaction significantly improves model fit, you can use model comparison.

m1 < - Imer(NoiseCond*WordCond + (1|Subject) + (1|Item)) m2 < - Imer(NoiseCond+WordCond + (1|Subject) + (1|Item)) anova(m1, m2)

Summary and Tips

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More About Interactions How you code your predictors determines which hypotheses you are testing.

- Think about what paired comparisons you are interested in testing prior to setting up a coding scheme.
- Choose your baselines carefully, and know what each coding variable is testing.
 - This will help you know which means/differences are being tested and what the sign of your coefficient represents.
- Would a variable you would treat as unordered and categorical in ANOVA be better served as an ordered variable (Helmert, Polynomial), or is it actually continuous?

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THANK YOU!!!

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